

## Notches in Fatigue

## Professor Darrell F. Socie University of Illinois at Urbana-Champaign

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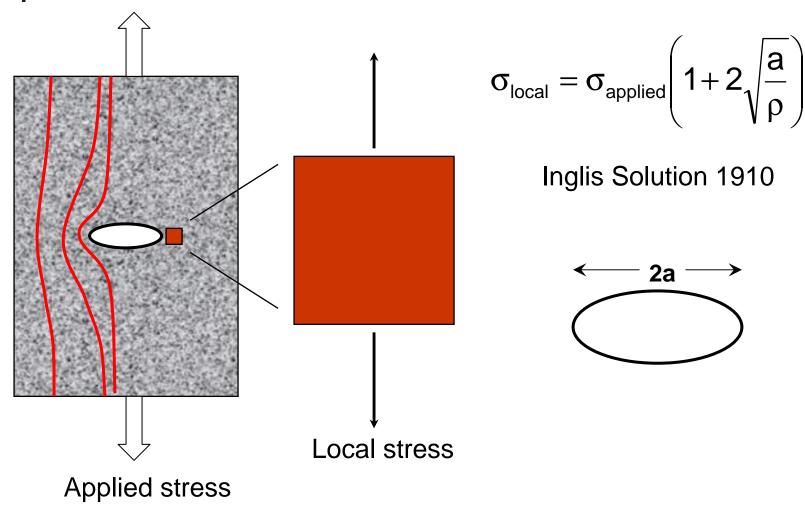


#### **Outline**

- 1. Notch Rules
- 2. Fatigue Notch Factor
- 3. Stress Intensity Factors for Notches
- 4. Frost Data and K<sub>f</sub>
- 5. Small Crack Growth
- 6. Small Notches



## **Stress Concentration Factor**





#### **Notch Rules**

#### Neuber

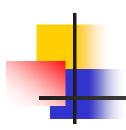
$$K_t^2 Se = \sigma \varepsilon = \frac{\sigma}{E} + \left(\frac{\sigma}{K}\right)^{\frac{1}{n}}$$
Glinka

$$K_t^2 Se = \int \sigma d\epsilon = \frac{\sigma}{E} + \frac{1}{1+n} \left(\frac{\sigma}{K}\right)^{\frac{1}{n}}$$

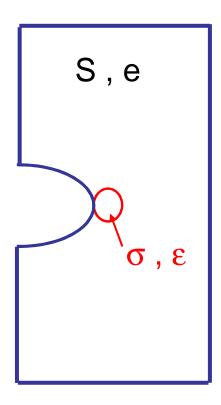
#### Seeger

$$K_p^2 S^* e^* = \sigma \epsilon = \frac{\sigma}{E} + \left(\frac{\sigma}{K}\right)^{\frac{1}{n}}$$

$$K_p = \frac{S_{Limit} K_t}{\sigma_y}$$
  $S^* = \frac{K_t}{K_p} S$ 



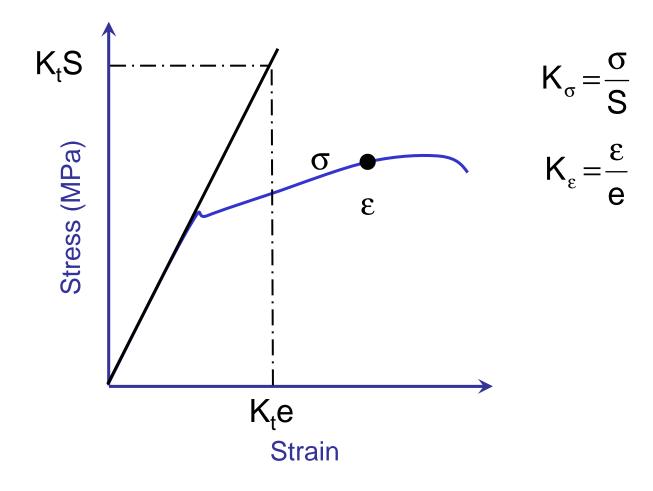
## Define $K_{\sigma}$ and $K_{\epsilon}$ after Yielding



Define: nominal stress, S nominal strain, e notch stress,  $\sigma$  notch strain,  $\epsilon$ 

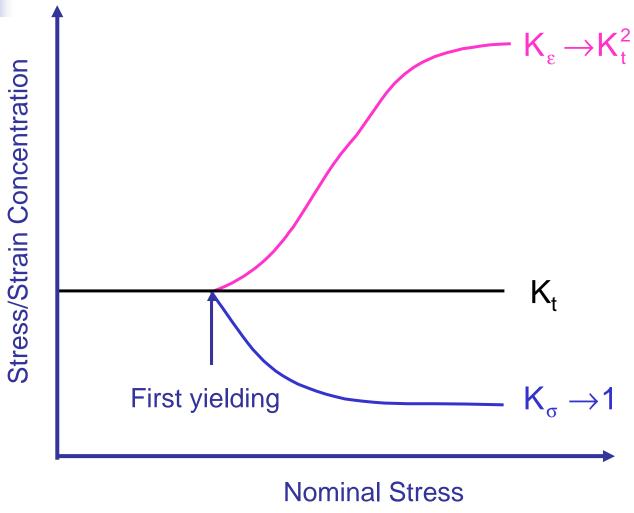
Stress concentration  $K_{\sigma} = \frac{c}{s}$ Strain concentration  $K_{\varepsilon} = \frac{\varepsilon}{e}$ 

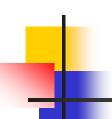
# $K_{\sigma}$ and $K_{\epsilon}$



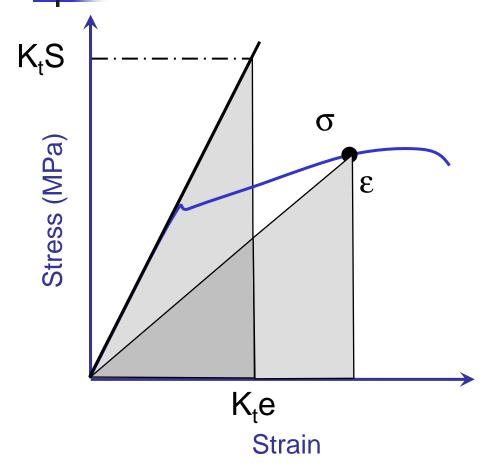


## Stress and Strain Concentration





## Neuber's Rule



**Actual stress** 

$$K_{t} S K_{t} e = \sigma \epsilon$$

Stress calculated with elastic assumptions



## Neuber's Rule for Fatigue

Stress and strain amplitudes

$$\frac{K_t \Delta S K_t \Delta e}{2} = \frac{\Delta \sigma \Delta \epsilon}{2 2}$$

Elastic nominal stress

$$\frac{\Delta e}{2} = \frac{\Delta S}{2E}$$

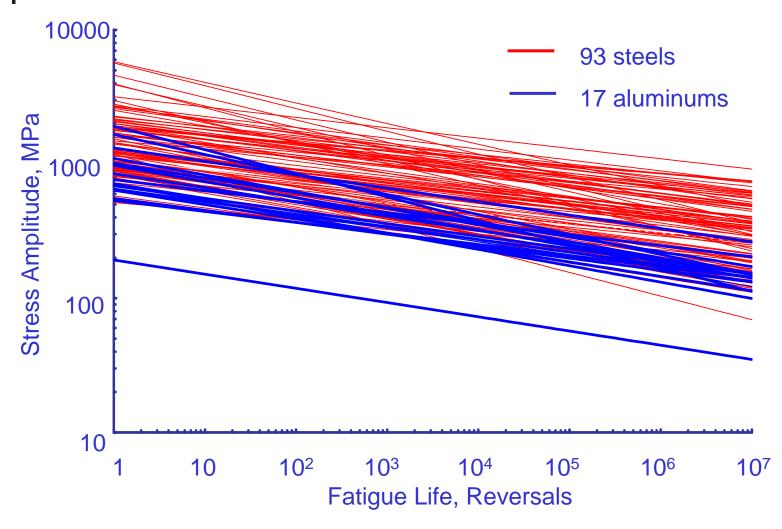
Substitute and rearrange

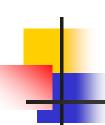
$$K_{t} \frac{\Delta S}{2} = \sqrt{E \frac{\Delta \sigma}{2} \frac{\Delta \epsilon}{2}}$$

The product of stress times strain controls fatigue life

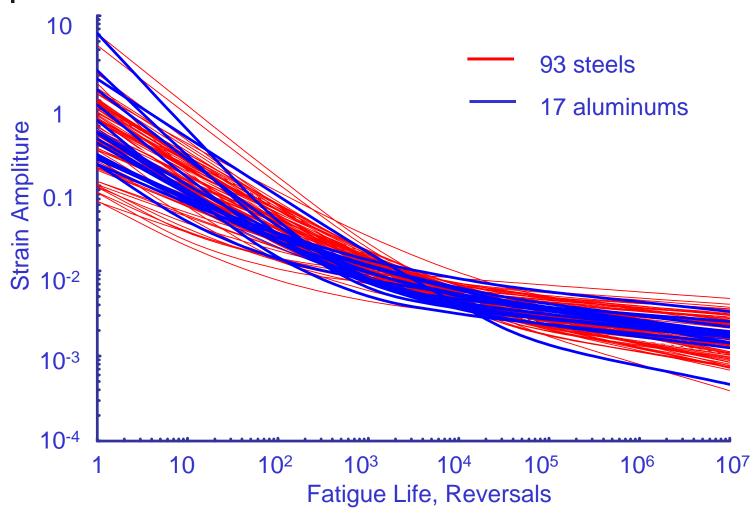


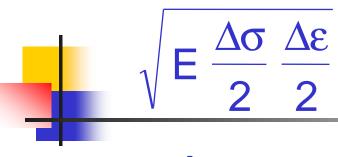
## **SN Materials Data**

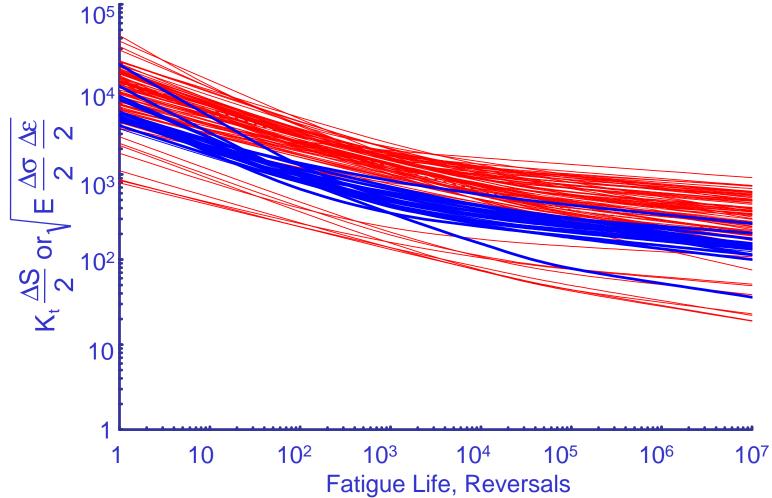




## εN Materials Data









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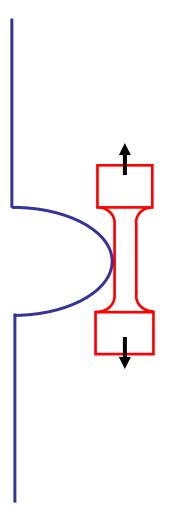
Stress analysis and stress concentration factors are independent of size and are related only to the ratio of the geometric dimensions to the loads

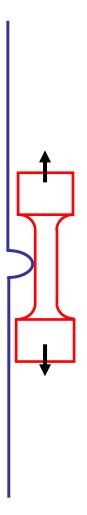
Fatigue is a size dependant phenomena

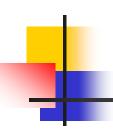
How do you put the two together?



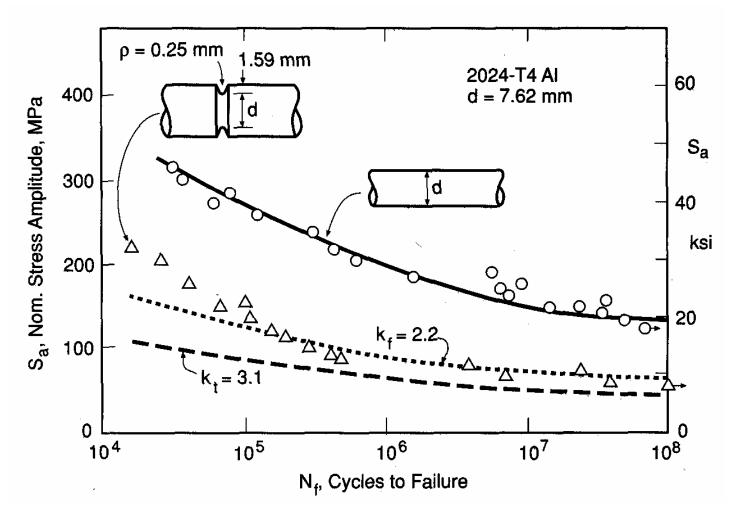
## Similitude



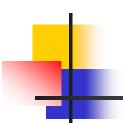




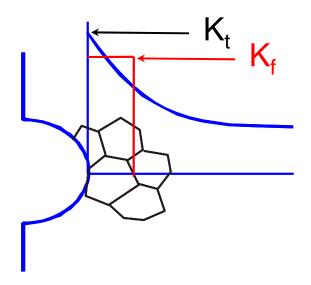
## Fatigue of Notches

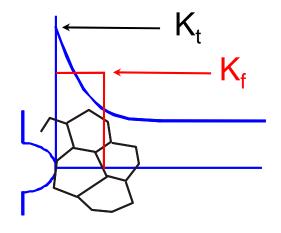


From Dowling, Mechanical Behavior of Materials, 1999



## **Notch Size**



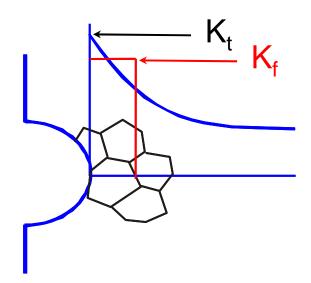


Large Notch

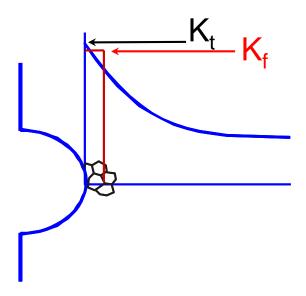
**Small Notch** 



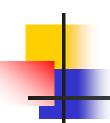
## Microstructure Size



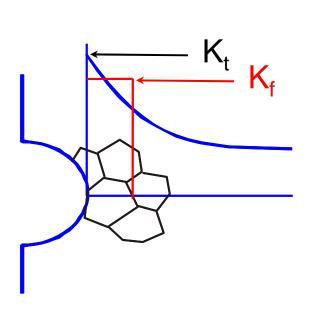
Low Strength



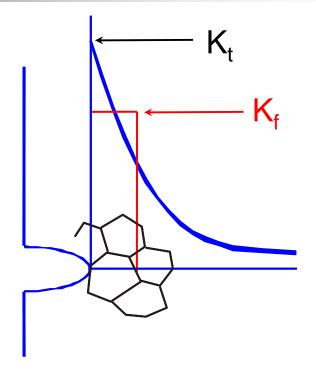
High Strength



## **Stress Gradient**

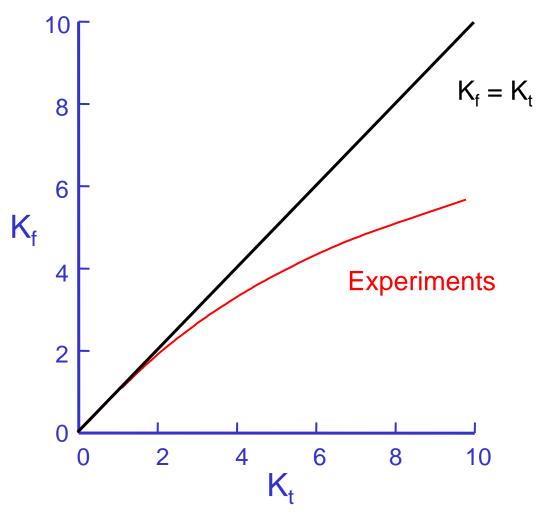






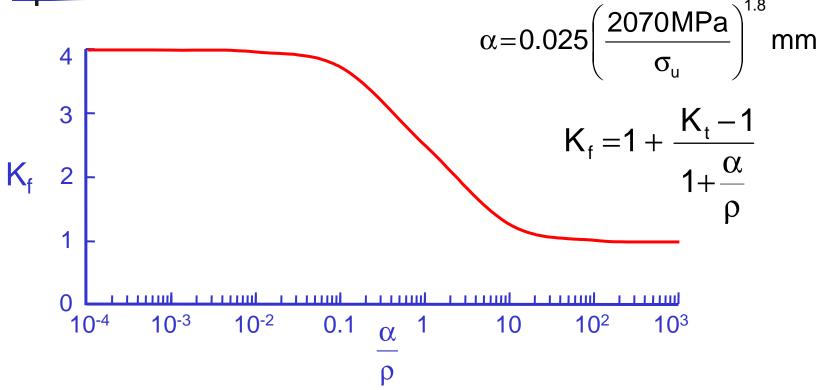
High K<sub>t</sub>





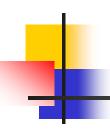


## Peterson's Equation

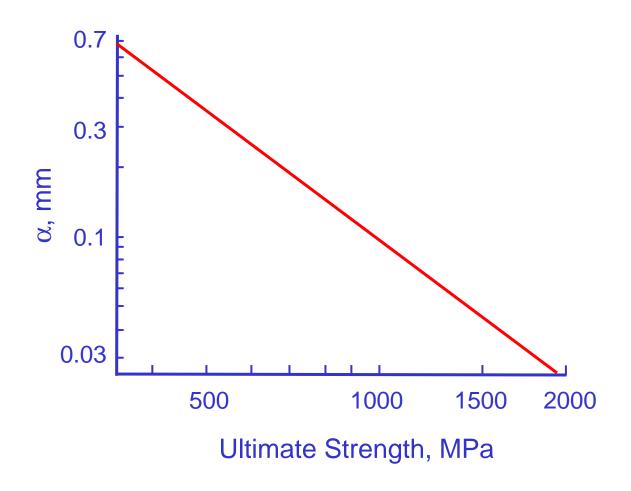


No effect when  $\rho \ll \alpha$ 

Full effect when  $\rho \gg \alpha$ 

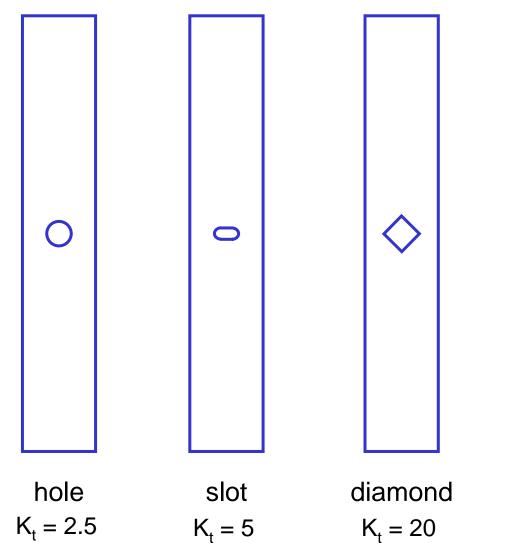


## Pererson's Constant





## Static Strength

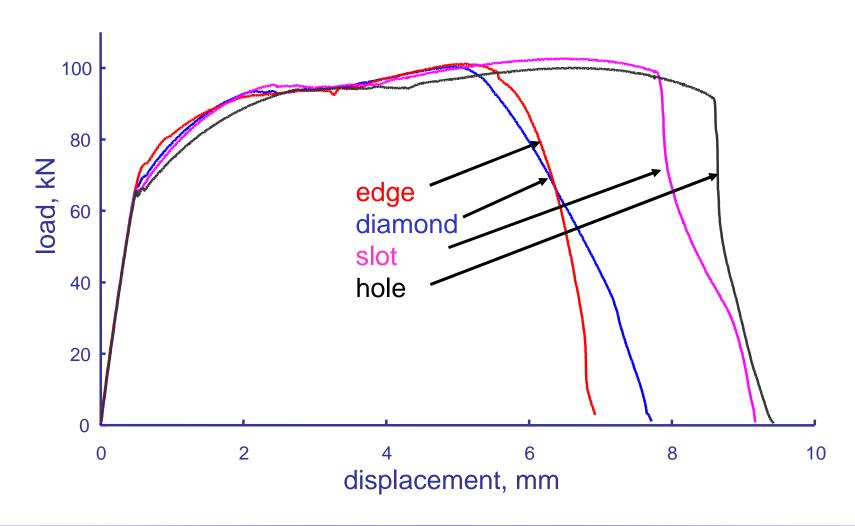


edge

 $K_{t} = 20$ 

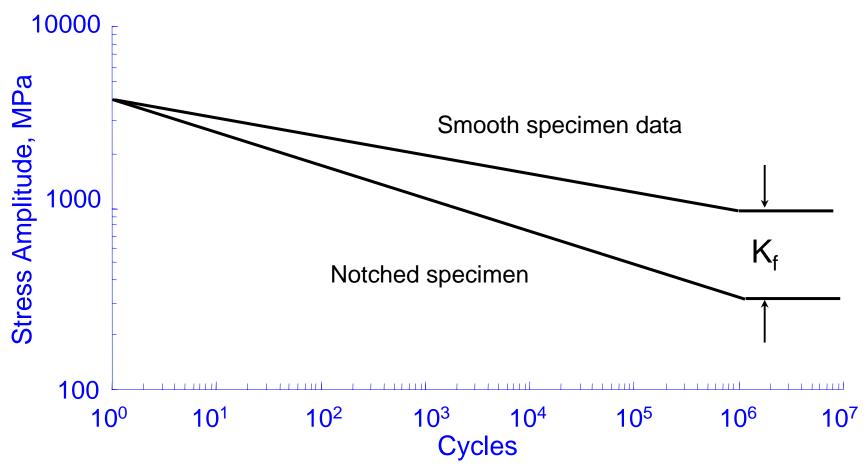


## 1018 Steel Test Data





### **Notched SN Curve**



Stress concentrations are not very important at short lives

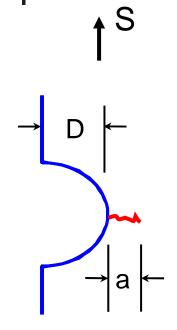


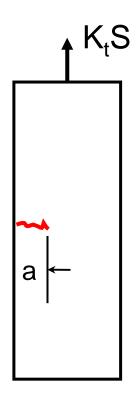
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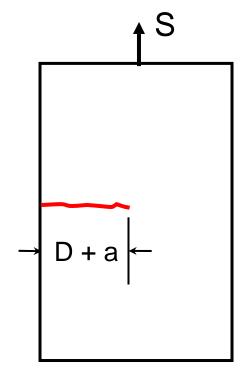


## **Cracks at Notches**



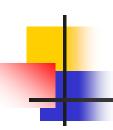


$$a \ll D$$
 $K = K_t S \sqrt{\pi a}$ 

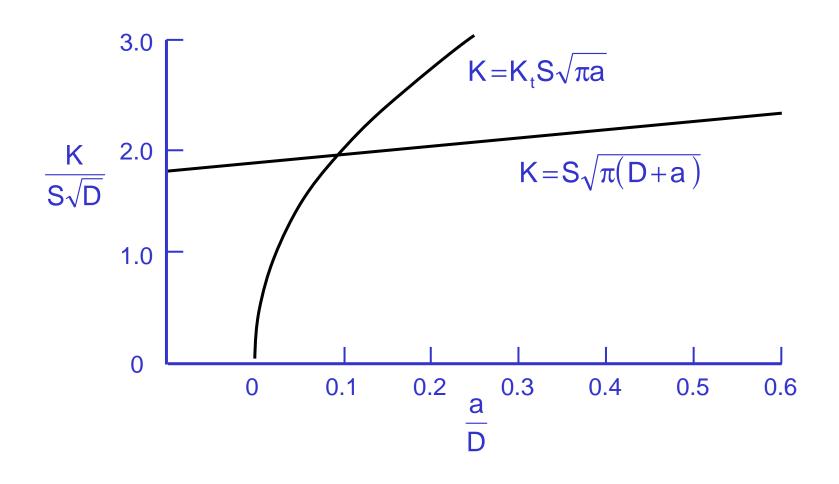


$$a \gg D$$

$$K = S\sqrt{\pi(D+a)}$$

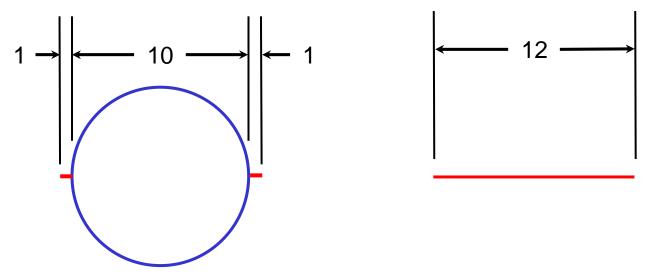


## **Stress Intensity Factors**





### Cracks at Holes



Once a crack reaches 10% of the hole radius, it behaves as if the hole was part of the crack

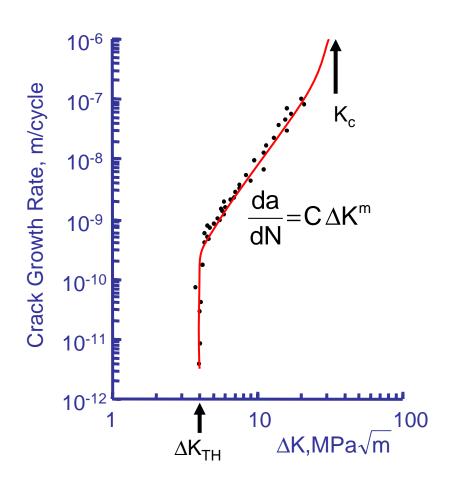


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## Crack Growth Data

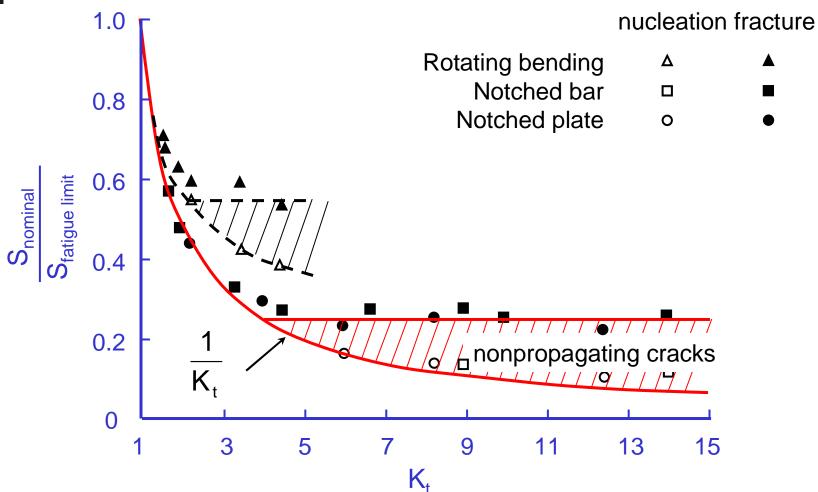


Nonpropagating cracks

$$\Delta K_{TH} > \Delta \sigma 1.12 \frac{2}{\pi} \sqrt{\pi a}$$



### **Frost Data**



Frost, "A Relation Between the Critical Alternating Propagation Stress and Crack Length for Mild Steel" Proceedings of the Institute for Mechanical Engineers, Vol. 173, No. 35, 1959, 811-836

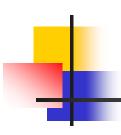


## Significance

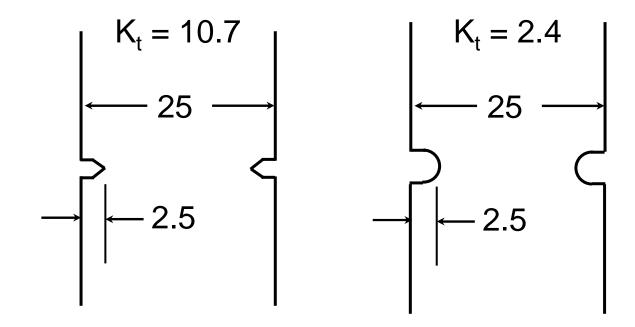
For  $K_t > 4$ , the notch acts like a crack with a depth D

$$\mathsf{S}_{\mathsf{fl}} = \frac{\Delta \mathsf{K}_{\mathsf{th}}}{\sqrt{\pi \mathsf{D}}}$$

K<sub>t</sub> does not play a role for sharp notches!



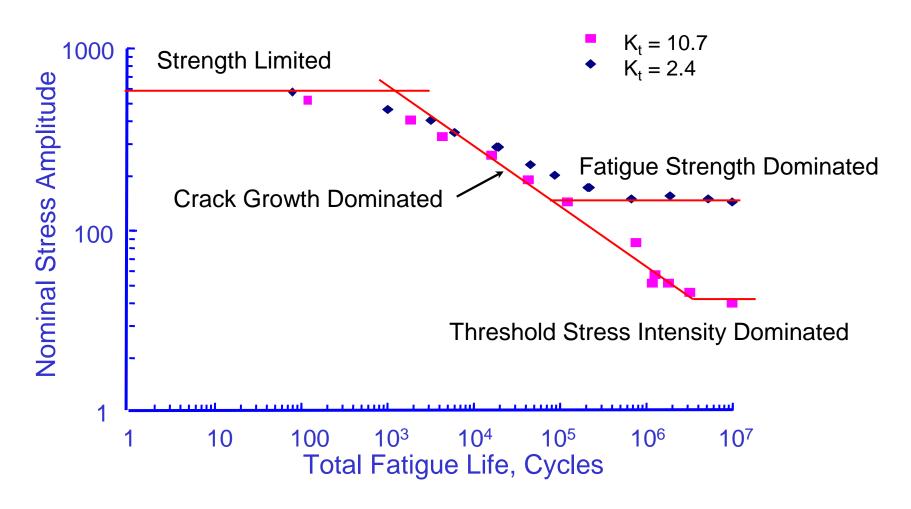
## Specimens with Similar Geometry



Ultimate Strength 780 MPa Yield Strength 660 MPa



## **Test Results**



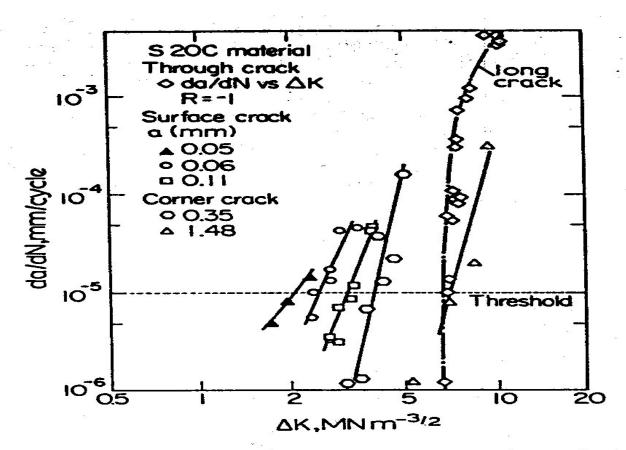


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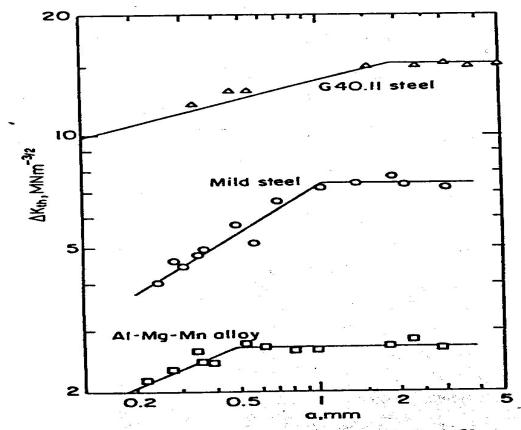
## **Small Crack Growth**



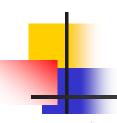
Difference in propagation rates da/dN of short and long fatigue cracks as function of stress intensity factor range  $\Delta K$  for 3%Si iron of yield strength  $\sigma_0 = 431$  MNm<sup>-2</sup> (Ref. 70)



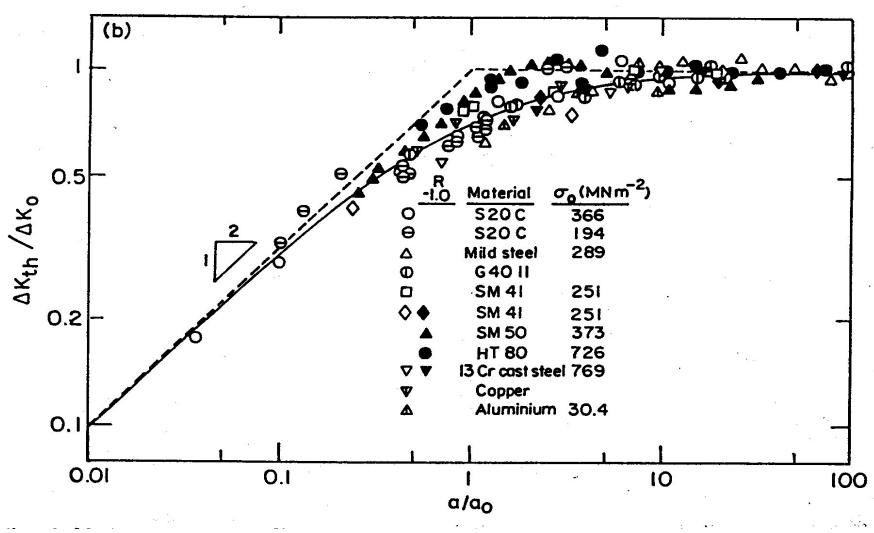
### **Threshold**



Variation of threshold stress intensity range  $\Delta K_{\rm th}$  with short crack length a in G40.11 austenitic 0.45%C steel,  $\sigma_0=550$  MNm<sup>-2</sup>, 0.035%C mild steel,  $\sigma_0=242$  MNm<sup>-2</sup>, and Al—Zn—Mg alloy,  $\sigma_0=180$  MNm<sup>-2</sup> (Ref. 69)

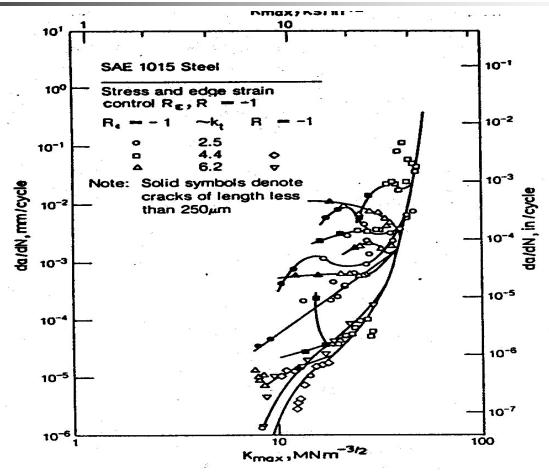


## Normalized Thresholds





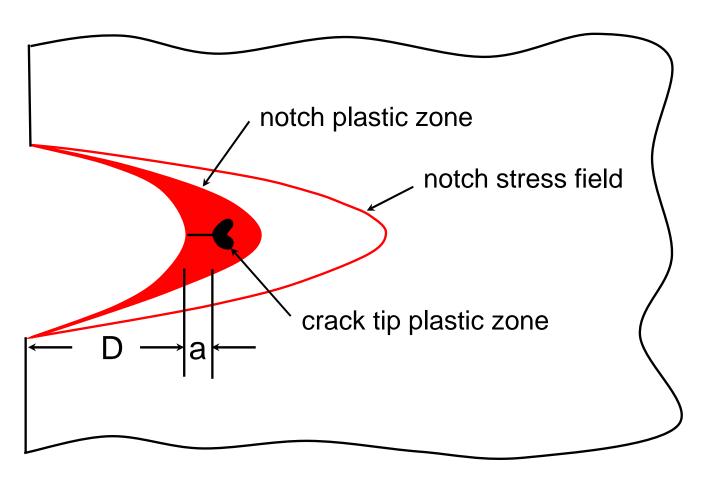
## **Growth from Notches**



Propagation rate da/dN of cracks emanating from notches as function of maximum stress intensity factor  $K_{\max}$  in 0.15%C mild steel;  $k_t$  is theoretical elastic stress concentration factor, R stress ratio, and  $R_{\epsilon}$  edge strain ratio<sup>110</sup>

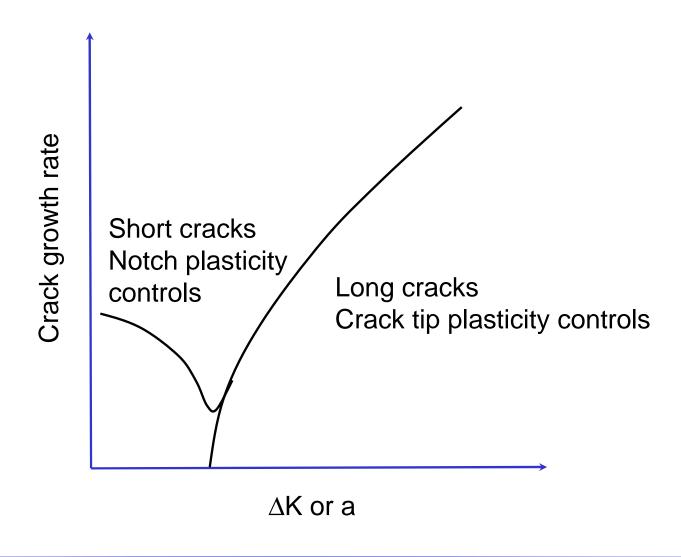


## Cracks at Notches



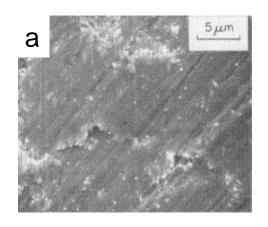


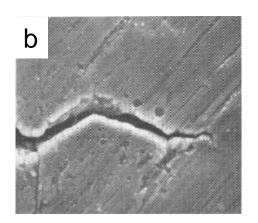
## **Crack Growth**

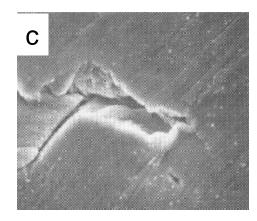


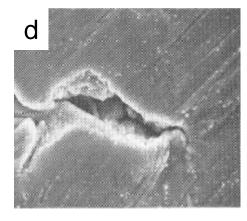


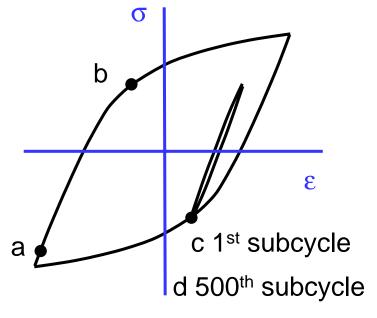
## **Closure Observations**











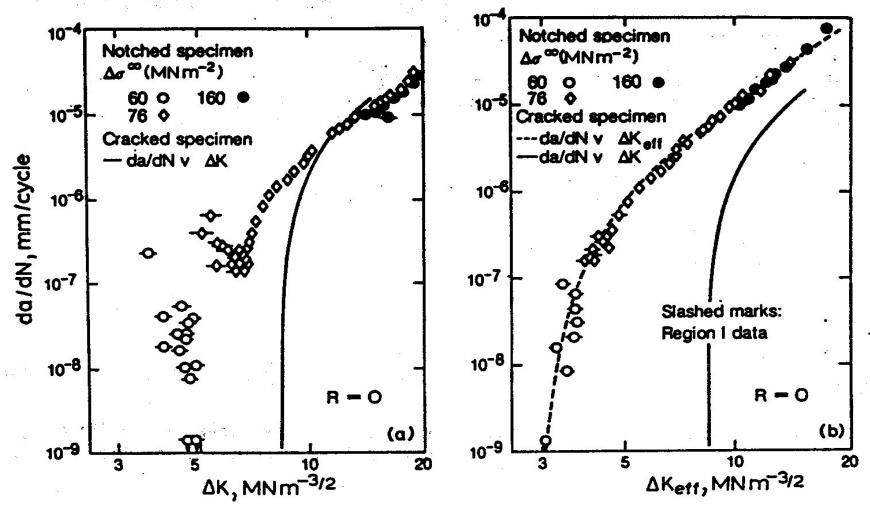
1026 steel

$$\Delta \varepsilon_1/2 = 0.005$$

$$\Delta \varepsilon_2/2 = 0.001$$



## Closure Correlation



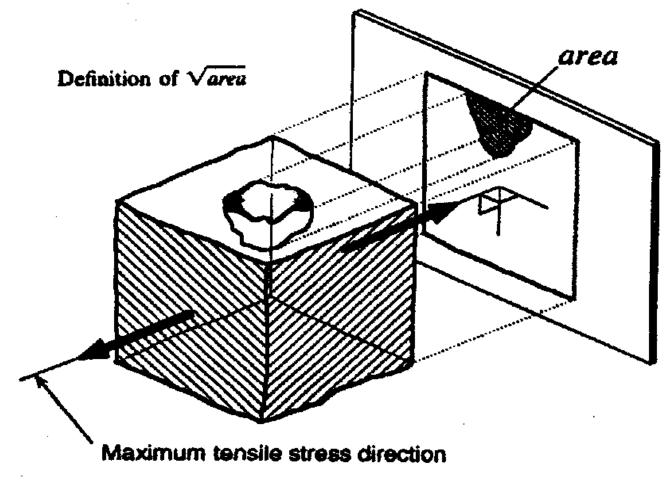


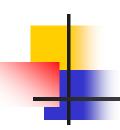
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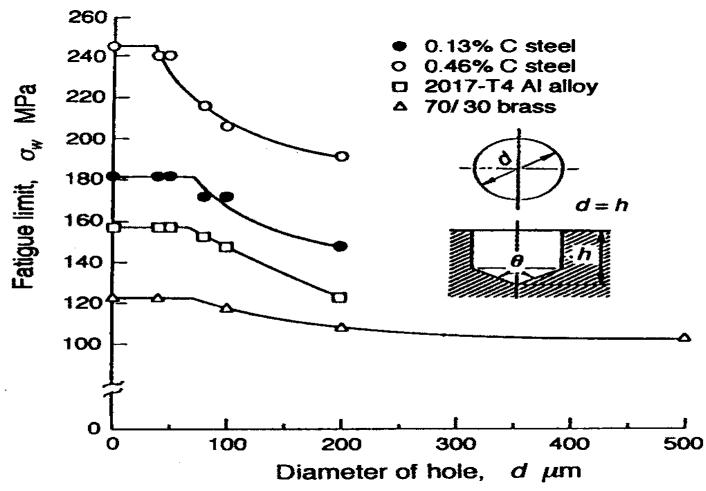






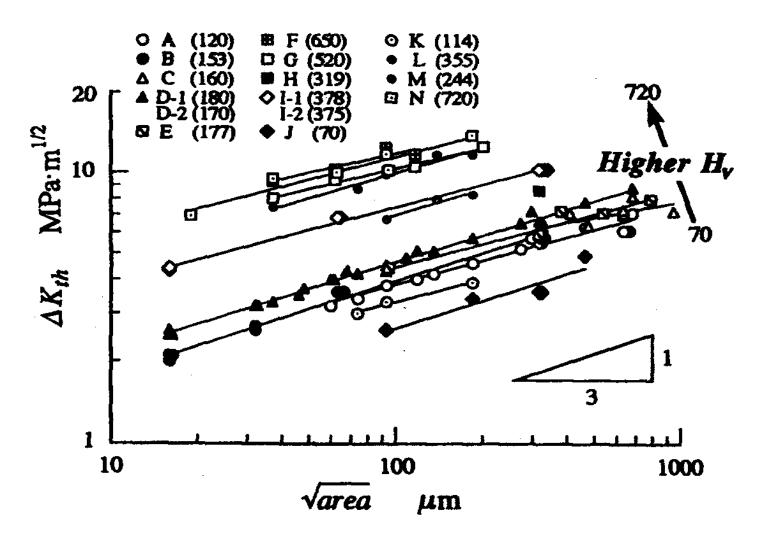


## **Small Notches**



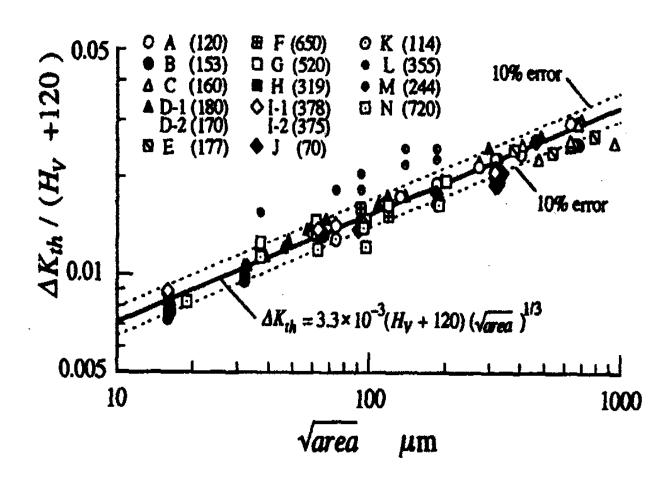


## Threshold Stress Intensity



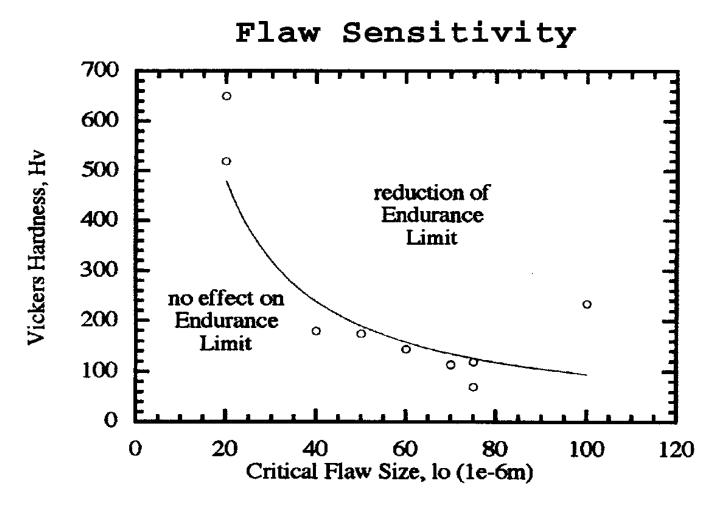


### **Hardness Corelation**



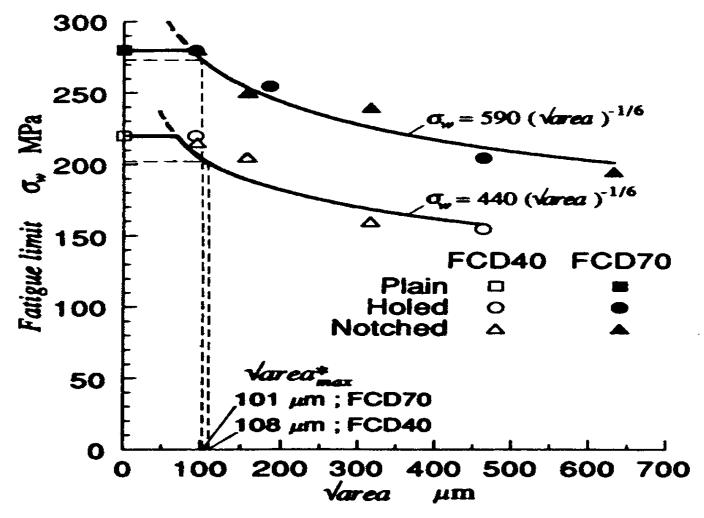


## Flaw Sensitivity





## **Fatigue Limit**



# **Notches in Fatigue**

